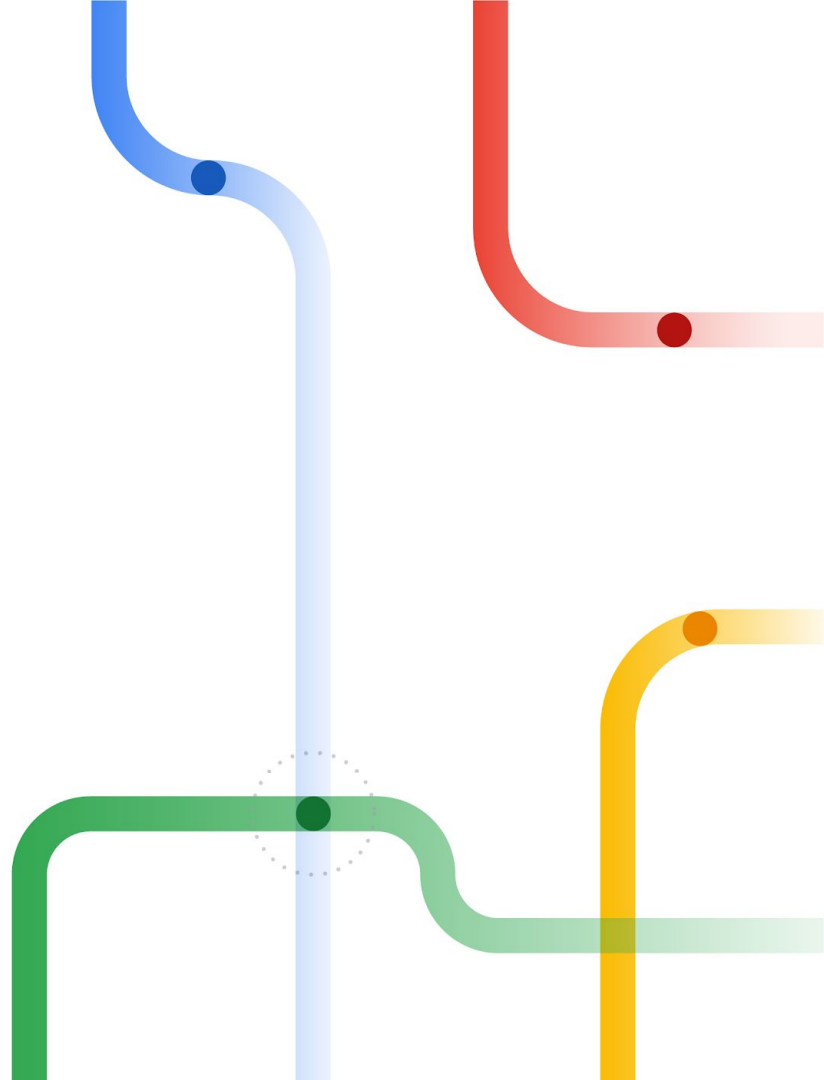


A tale of two encoders for neural retrieval

Aditya Krishna Menon

Sep 5th, 2024

Google Research



About me

Research Scientist at Google NYC

Working on machine learning algorithm design and analysis



Past lives:

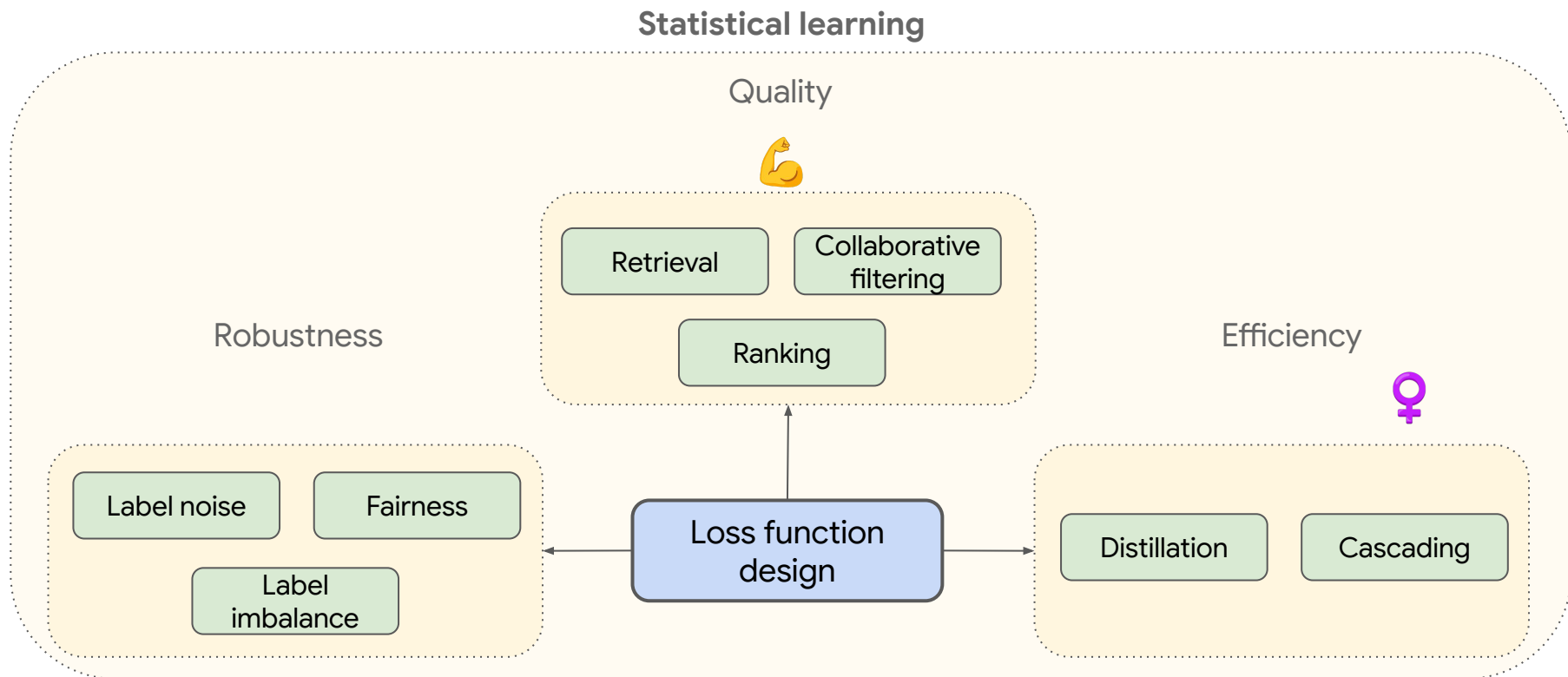
- University of Sydney
- UC San Diego
- NICTA / CSIRO Data61 / Australian National University



DATA
61



About my work



About this talk

Summary of (some of) our team's (+ collaborators') work on [neural retrieval](#)



Ankit Singh
Rawat



Andreas Veit



Felix Yu



Himanshu Jain



Manzil Zaheer



Rama
Pasumarthi



Rob Fergus



Sadeep
Jayasumana



Sanjiv Kumar



Sashank Reddi



Seungyeon Kim



Veeru
Sadhanala



Wittawat
Jitkrittum



Ziwei Ji

Agenda

- 01 **A (neural) retrieval primer**
- 02 Limits of dual encoders
- 03 Unified cross & dual encoders
- 04 Hybrid cross & dual encoders
- 05 Conclusion & future work

Information retrieval

- Given a query, and an item corpus, find the k most relevant items

“books with sad endings”



Retrieval phase

- Typically, we first retrieve a set of candidate items

“books with sad endings”



Re-ranking phase

- We then **re-rank** these items to obtain the final results

“books with sad endings”



Re-ranking phase

- We then **re-rank** these items to obtain the final results

“books with sad endings”



Re-ranking phase

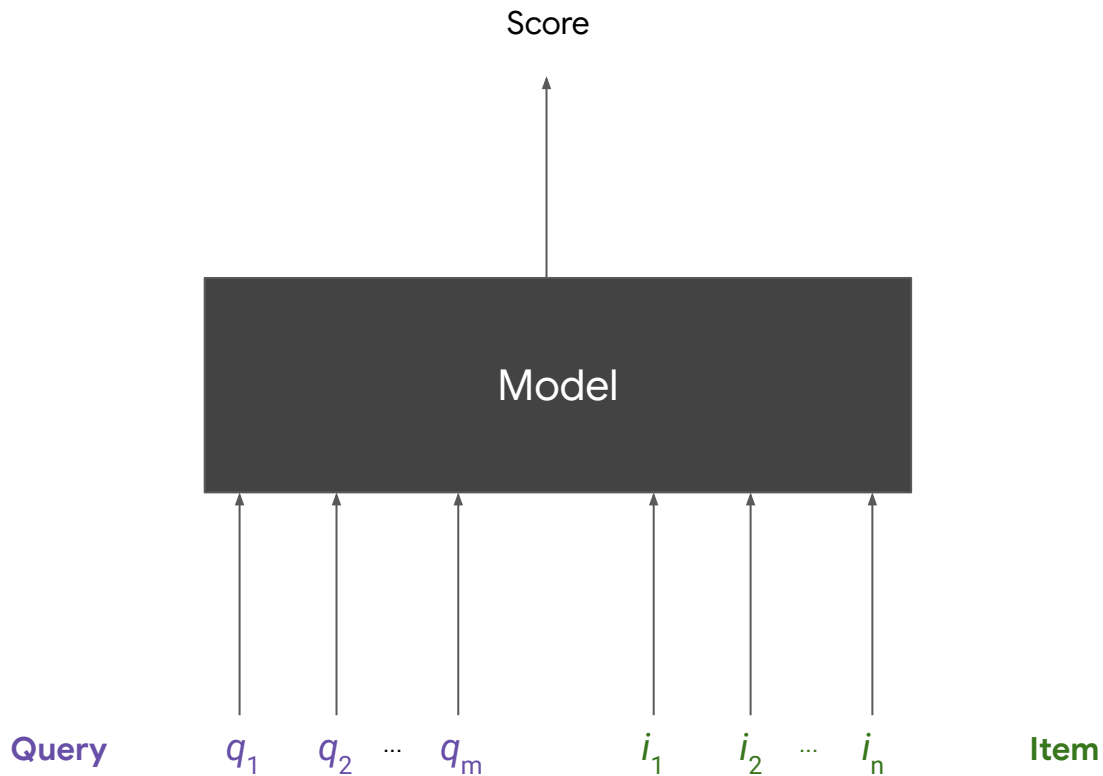
- We then **re-rank** these items to obtain the final results

“books with sad endings”



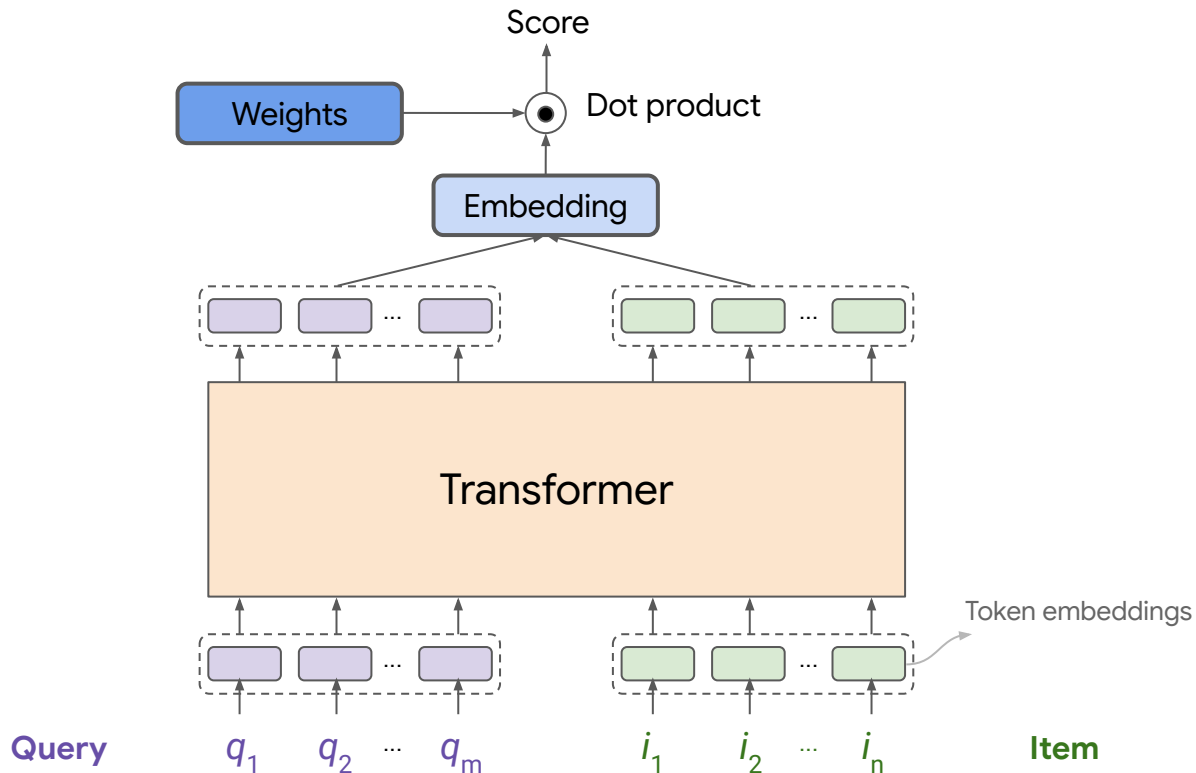
Encoder-based models

- In both phases, we need to score (Query, Item) affinity



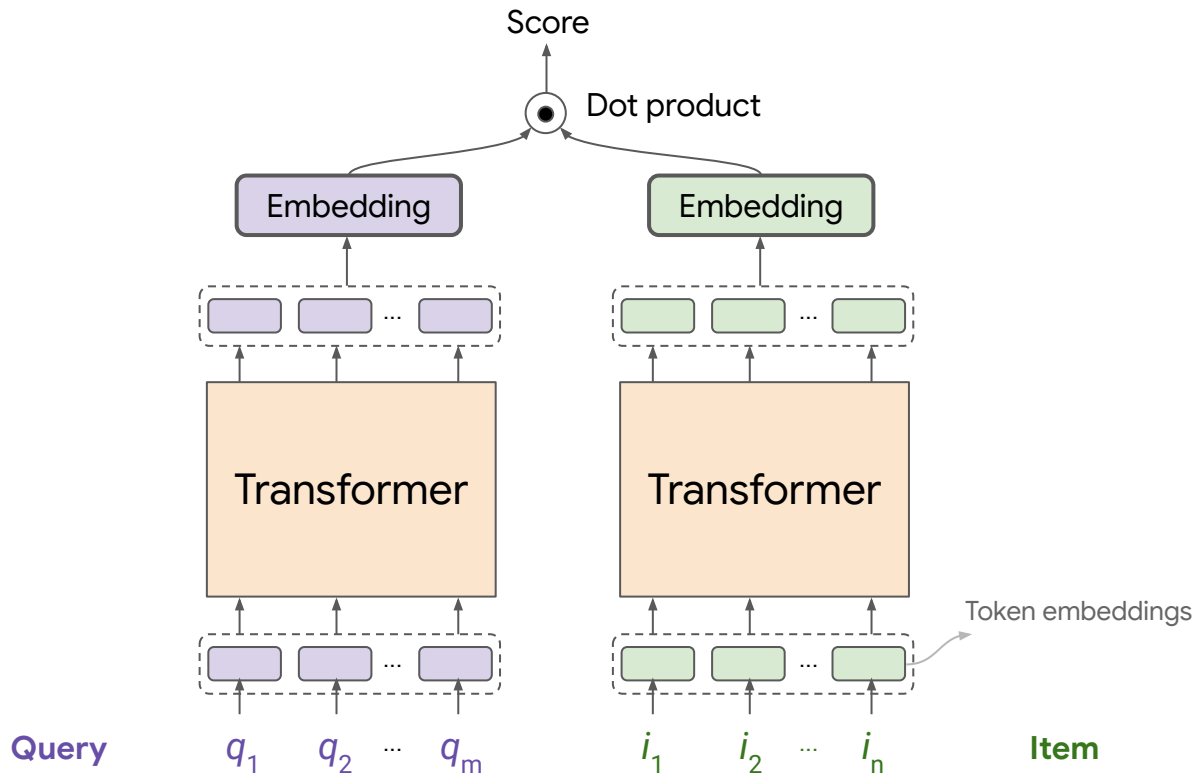
Cross-encoders

- Cross-encoders **jointly** embed queries and items, and project the embedding



Dual-encoders

- Dual-encoders **separately** embed queries and items, and measure embedding similarity



Encoder training

- Each query may have one or more associated **positive** items
 - Natively, a (featurised) multi-label learning problem



- Can create a **set of multi-class labels** for each positive
 - Now amenable to, e.g., softmax cross-entropy
 - Key challenge becomes suitable **negative mining**



Cross- versus dual-encoders

Dual-encoders are highly efficient for [retrieval](#); cross-encoders inapplicable!

Dual-encoders tend to underperform for [re-ranking](#)

Model	MSMARCO re-rank		TREC DL19 re-rank		NQ re-rank	
	MRR	nDCG	MRR	nDCG	MRR	nDCG
Cross-attention BERT (12-layer)	0.370	0.430	0.829	0.749	0.746	0.673
Dual-encoder BERT (6-layer)	0.310	0.360	0.834	0.677	0.676	0.601

Maintain separate retrieval and re-ranking models

Cross- versus dual-encoders

Dual-encoders are highly efficient for **retrieval**; cross-encoders inapplicable!

Dual-encoders tend to underperform for **re-ranking**

Model	MSMARCO				NQ re-rank	
	MRR	nDCG@10	Recall@10	Recall@100	MRR	nDCG
Cross-attention BERT (12-layer)	0.746	0.673	0.834	0.677	0.676	0.601
Dual-encoder BERT (6-layer)	0.310	0.360	0.834	0.677	0.676	0.601

Is there more to the story?

Maintain separate retrieval and re-ranking models

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- 01 A (neural) retrieval primer
- 02 **Limits of dual encoders**
- 03 Unified cross & dual encoders
- 04 Hybrid cross & dual encoders
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Why does this happen?

Inherent capacity limit?

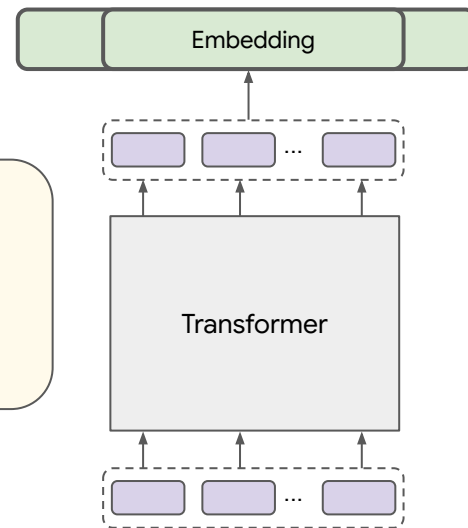
Limitations of training procedure?

...

Capacity of dual-encoders: theory

- Can dual-encoders fit any (reasonable) relevance function?

Proposition. Under mild technical conditions, any continuous query-item score function $s(q, i)$ can be approximated by some $Z(q)^T W(i)$, where $Z(q)$, $W(i)$ have at most **countably infinite** dimension.



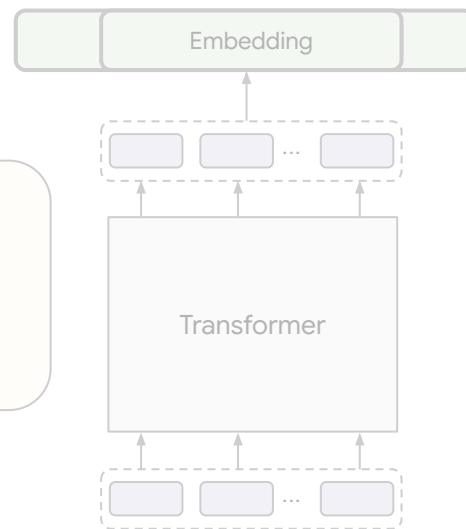
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- Can dual-encoders fit any (reasonable) relevance function?

Prop

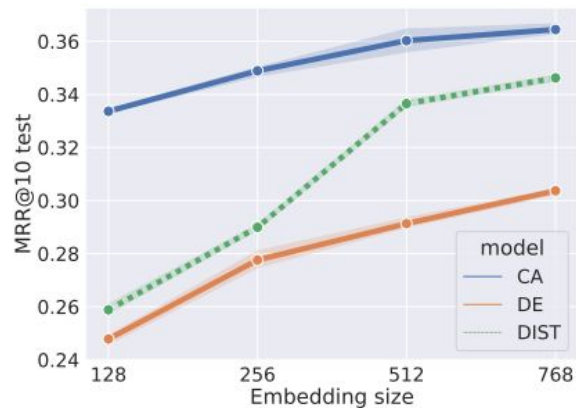
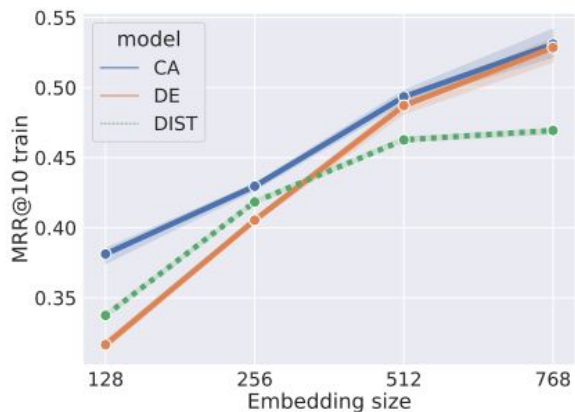
continuous query relevance function $\sigma(q, i)$ can be approximated by some $Z(q)^T W(i)$, where $Z(q), W(i)$ have at most **countably infinite** dimension.

Do we see this in practice?



Capacity of dual-encoders: practice

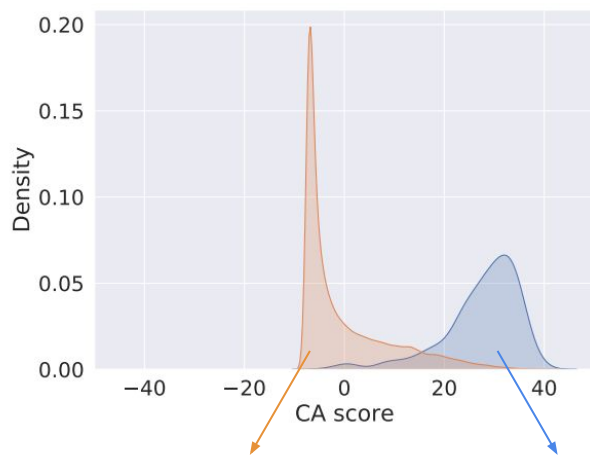
- With large embedding size, dual-encoders work well on **training** set!



BERT-based encoders on
MSMARCO

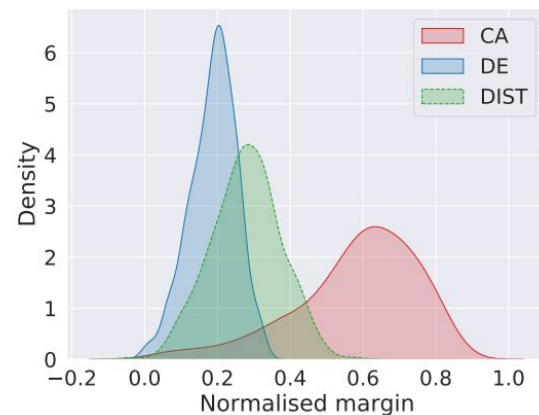
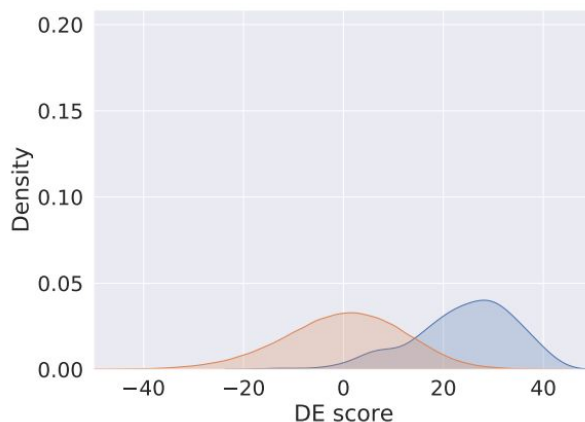
Why is there a generalisation gap?

- Dual-encoders tend to yield poorer margins
 - i.e., poorer gaps between score on positive and negative items



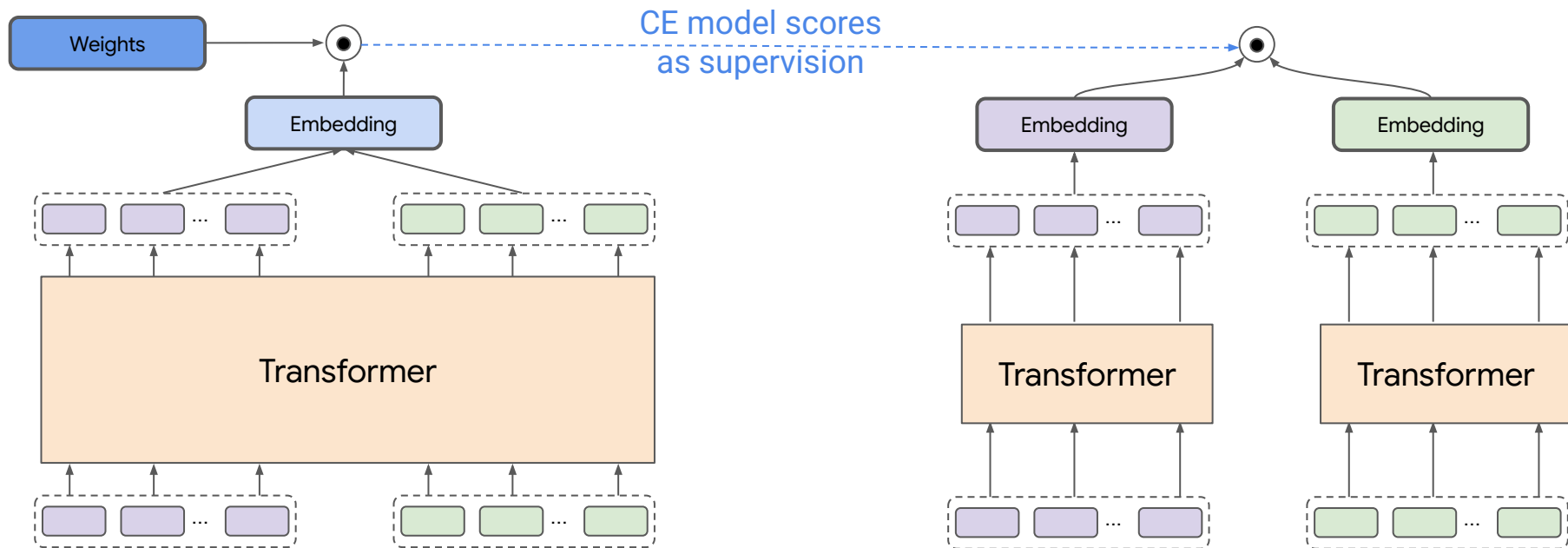
Negative

Positive



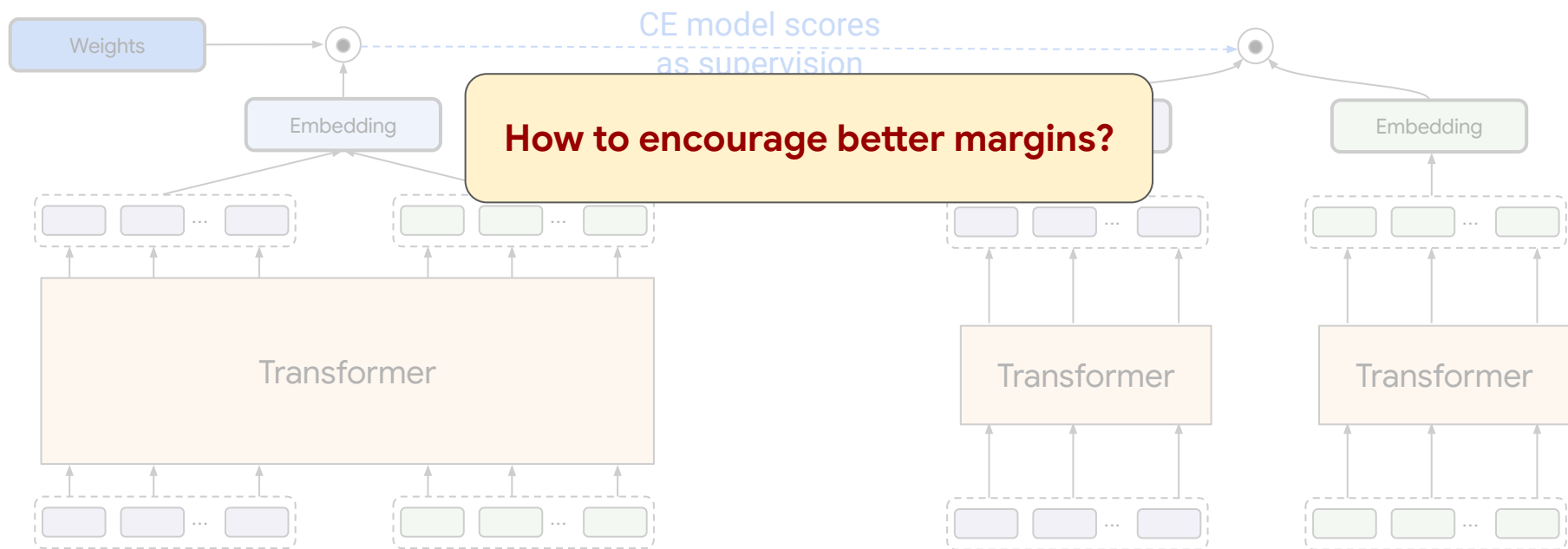
How can we mitigate the generalisation gap?

- **Distill** predictions from a cross-encoder “teacher” to dual-encoder “student”



How can we mitigate the generalisation gap?

- Distill predictions from a cross-encoder “teacher” to dual-encoder “student”

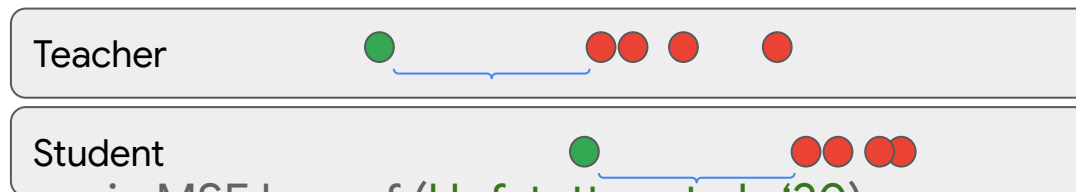


Distillation via multi-margin MSE (M³SE)

- Encourage **matching teacher margin** on positives P :

$$\ell_{\text{m}^3\text{se}}(\mathbf{t}, \mathbf{s}) = \sum_{i \in P} \left(\overset{\text{Teacher score}}{(t_i - t_{j^*})} - \overset{\text{Student score}}{(s_i - s_{j^*})} \right)^2 + \sum_{j \in N} [s_j - s_{j^*}]_+^2$$

Highest scoring negative

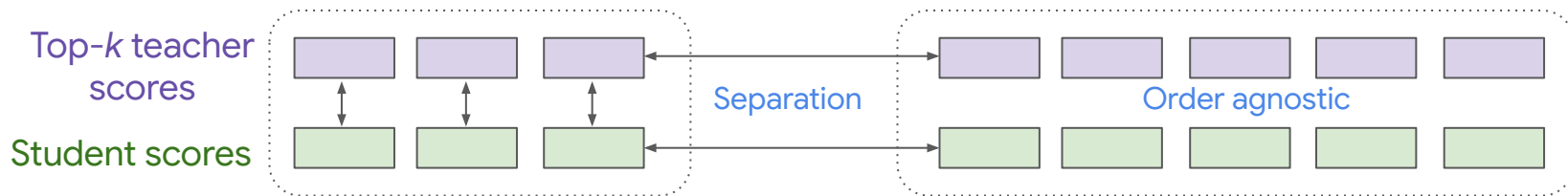


- Generalises margin MSE loss of (Hofstatter et al., '20)
 - For a single positive and negative, limiting case of softmax cross-entropy

Distillation via ranking matching

- More generally, we may seek to match teacher's **ranking** over **top-k** items
- Several versions of **RankDistil** objective possible:

$$\ell_{\text{RANKDISTIL}}(t, s, P, N) = \overset{\text{Multi-class loss}}{\Psi(t, s, P)} + \sum_{i \in N} \varphi(-s_i),$$
$$\ell_{\text{RANKDISTIL}}(t, s, P, N) = \Psi(t, s, P) + \sum_{i \in N} \sum_{j \in P} \overset{\text{Binary loss}}{\varphi(s_j - s_i)}$$



Empirical results for re-ranking

- Distillation can help mitigate the generalisation gap!

Model	MSMARCO re-rank		TREC DL19 re-rank		NQ re-rank	
	MRR	nDCG	MRR	nDCG	MRR	nDCG
One-hot models						
BM25 (Robertson & Zaragoza, 2009)	0.194 [†]	0.241 [†]	0.689 [†]	0.501 [†]	—	—
ANCE (Xiong et al., 2021)	—	—	—	—	0.677 [†]	—
Cross-attention BERT (12-layer)	0.370	0.430	0.829	0.749	0.746	0.673
Dual-encoder BERT (6-layer)	0.310	0.360	0.834	0.677	0.676	0.601
Distilled dual-encoders						
MSE (Hofstätter et al., 2020a)	0.289	0.343	0.781	0.693	0.659	0.591
Margin MSE (Hofstätter et al., 2020a)	0.334	0.392	0.867 [◇]	0.718	0.673	0.594
RankDistil-B (Reddi et al., 2021)	0.249	0.301	0.852	0.708	0.649	0.561
Softmax CE (Equation 1)	0.346	0.405	0.846	0.726 [◇]	0.682	0.607
M ³ SE (Equation 4)	0.349	0.406	0.852	0.714	0.699	0.625

Cross- versus dual-encoders

Dual-encoders tend to underperform for [re-ranking](#)

Model	MSMARCO re-rank		TREC DL19 re-rank		NQ re-rank	
	MRR	nDCG	MRR	nDCG	MRR	nDCG
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Poorer margins

Expressivity with small dimension

What can we do about it?

Distillation



Cross- versus dual-encoders

Dual-encoders tend to underperform for re-ranking

Model	MSMARCO re-rank		TREC DL19 re-rank		NQ re-rank	
	MRR	nDCG	MRR	nDCG	MRR	nDCG
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Can we make deeper changes?

Poorer margins

Expressivity with small dimension

What can we do about it?

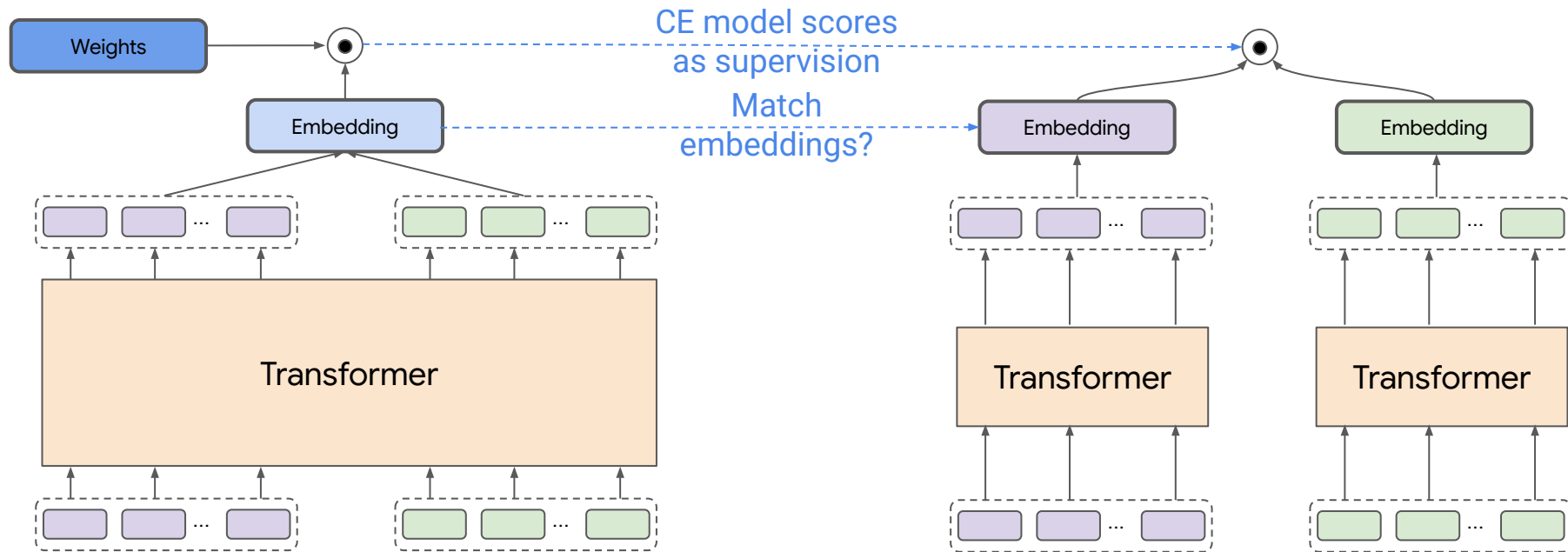
Distillation



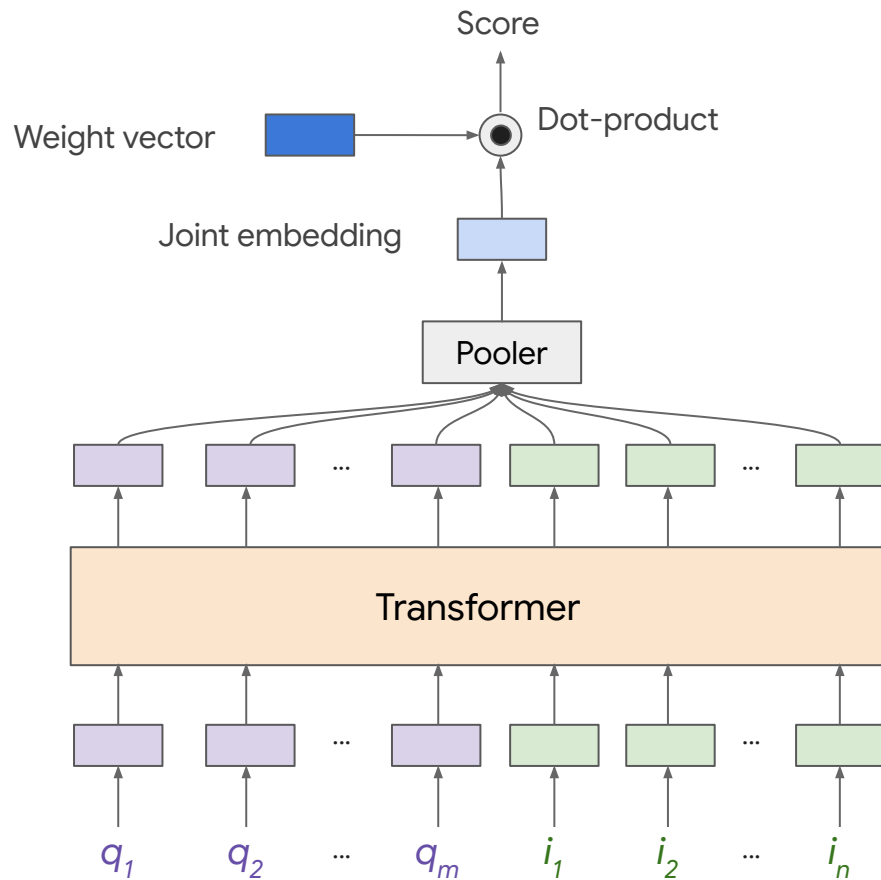
Agenda

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- 03 **Unified cross & dual encoders**
- 04 Hybrid cross & dual encoders
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Cross- to dual-encoder distillation



Cross-encoder embeddings: a closer look



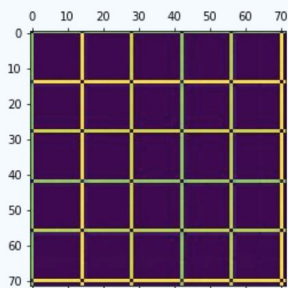
Do joint embeddings capture semantic structure?

Query + item tokens

The perils of (naïve) pooling

- Cross-encoder training seeks to align embeddings of:
 - **Positive** pairs with some (learned) weight vector w
 - **Negative** pairs with some (learned) weight vector $-w$
- Joint embeddings tend to not capture semantic structure!
 - No explicit coupling amongst embeddings within a group

Pairwise
distance matrix



[CLS]-pooled

All positive
 (q, d^+) pairs

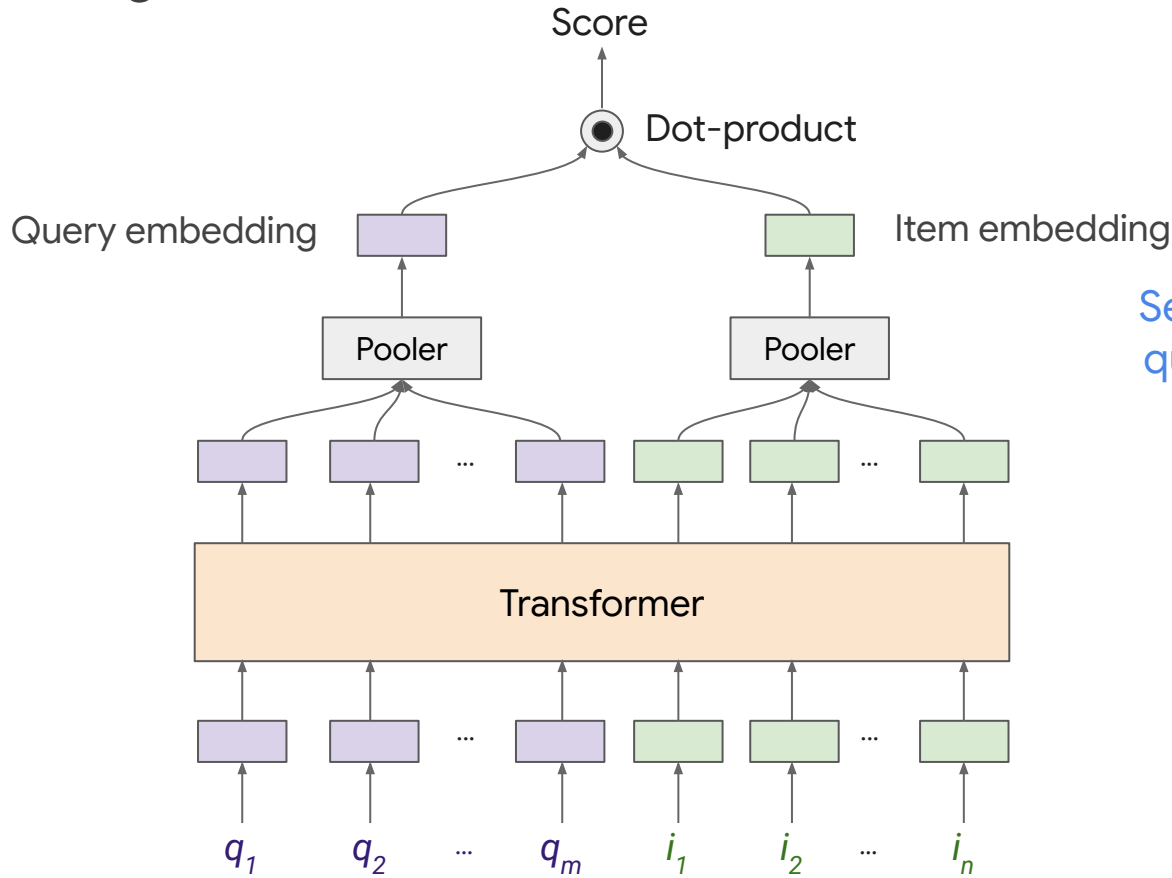


All negative
 (q, d^-) pairs




[CLS]-pooled CE model

The dual pooling trick

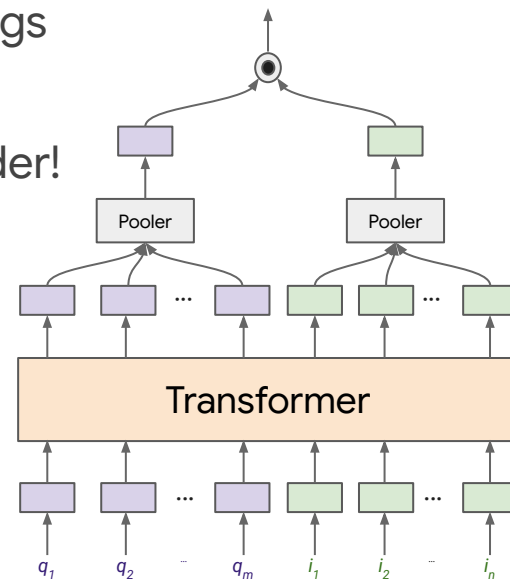


Separately pool
query and item
tokens!

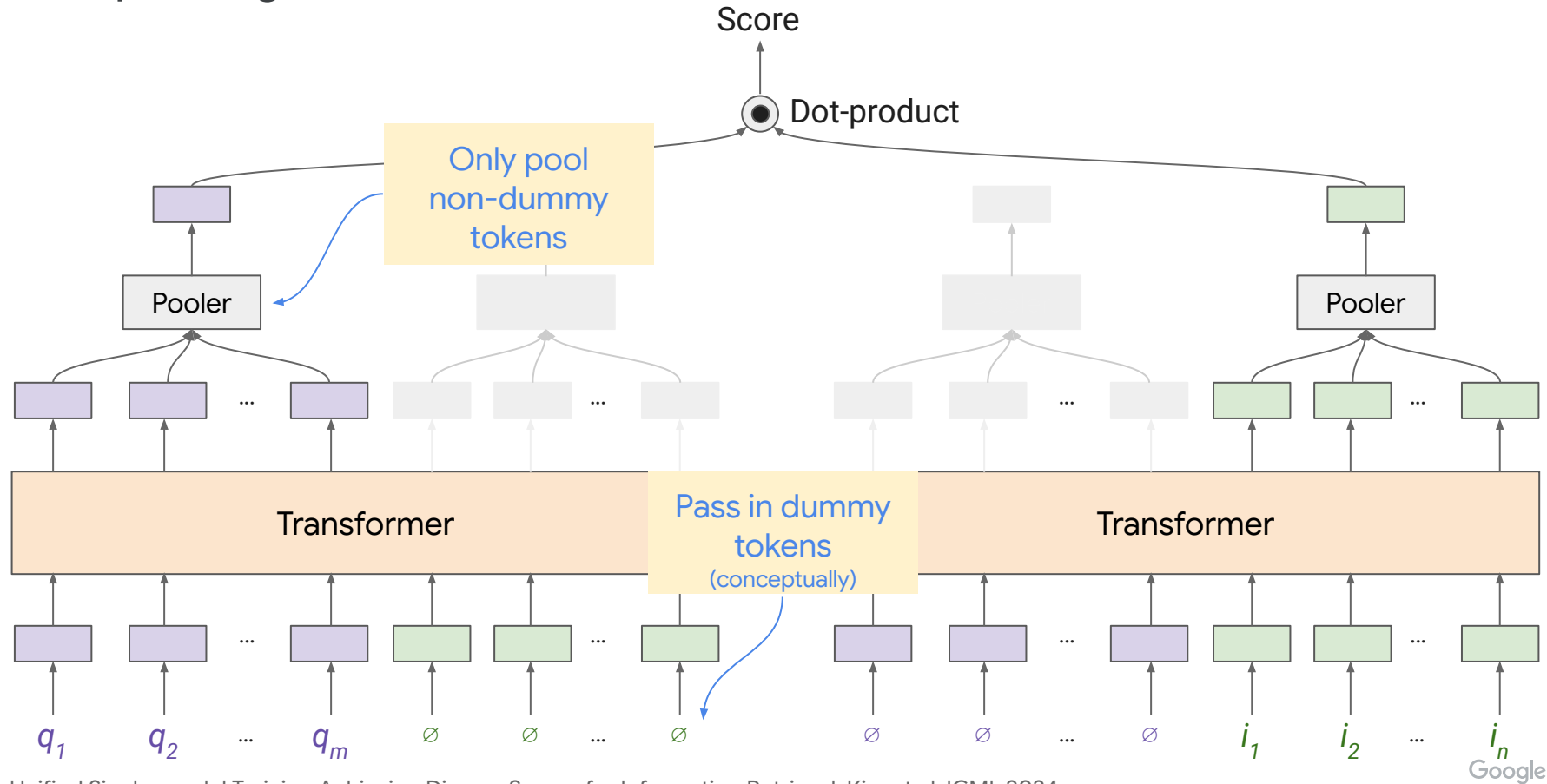
Query + item
tokens 

Dual pooling = dual encoder?

- Dual pooling produces separate query and item embeddings
- However, these involve joint processing through the encoder!
 - Not suitable for use as a dual encoder!
 - Cannot use this for efficient query → item search
- Need to separately process queries and items...

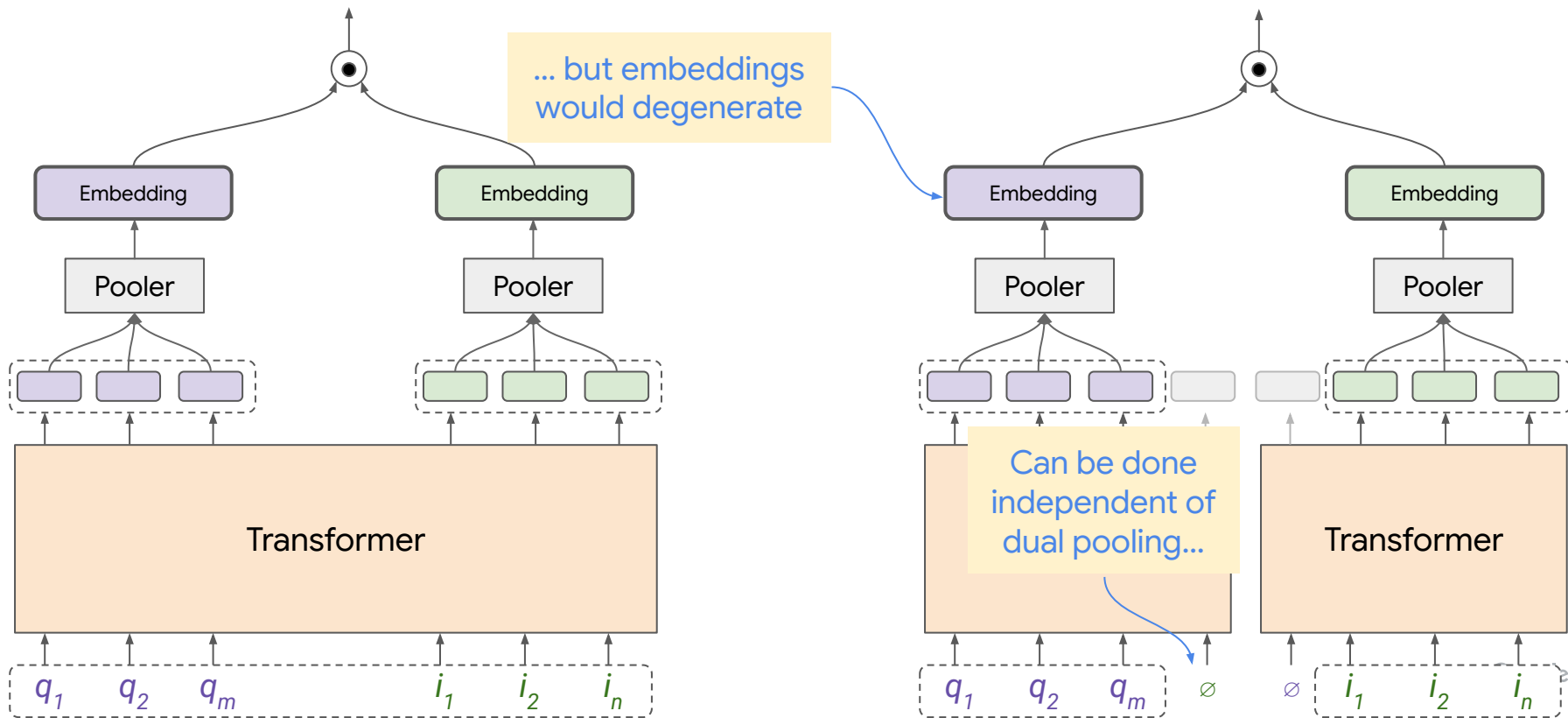


Dual pooling for dual-encoders



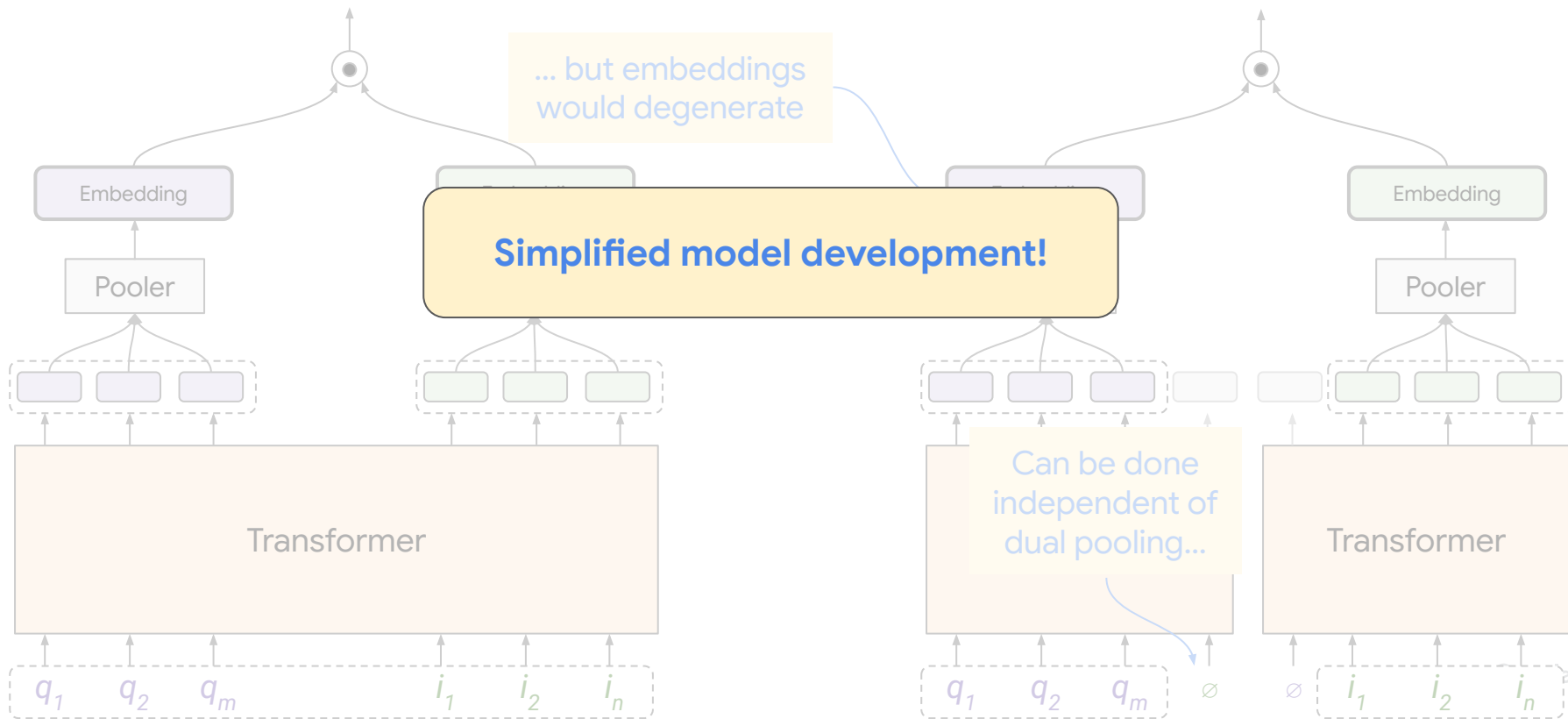
USTAD: unified cross- and dual-encoder

- Re-use same Transformer for both cross- and dual-encoder!



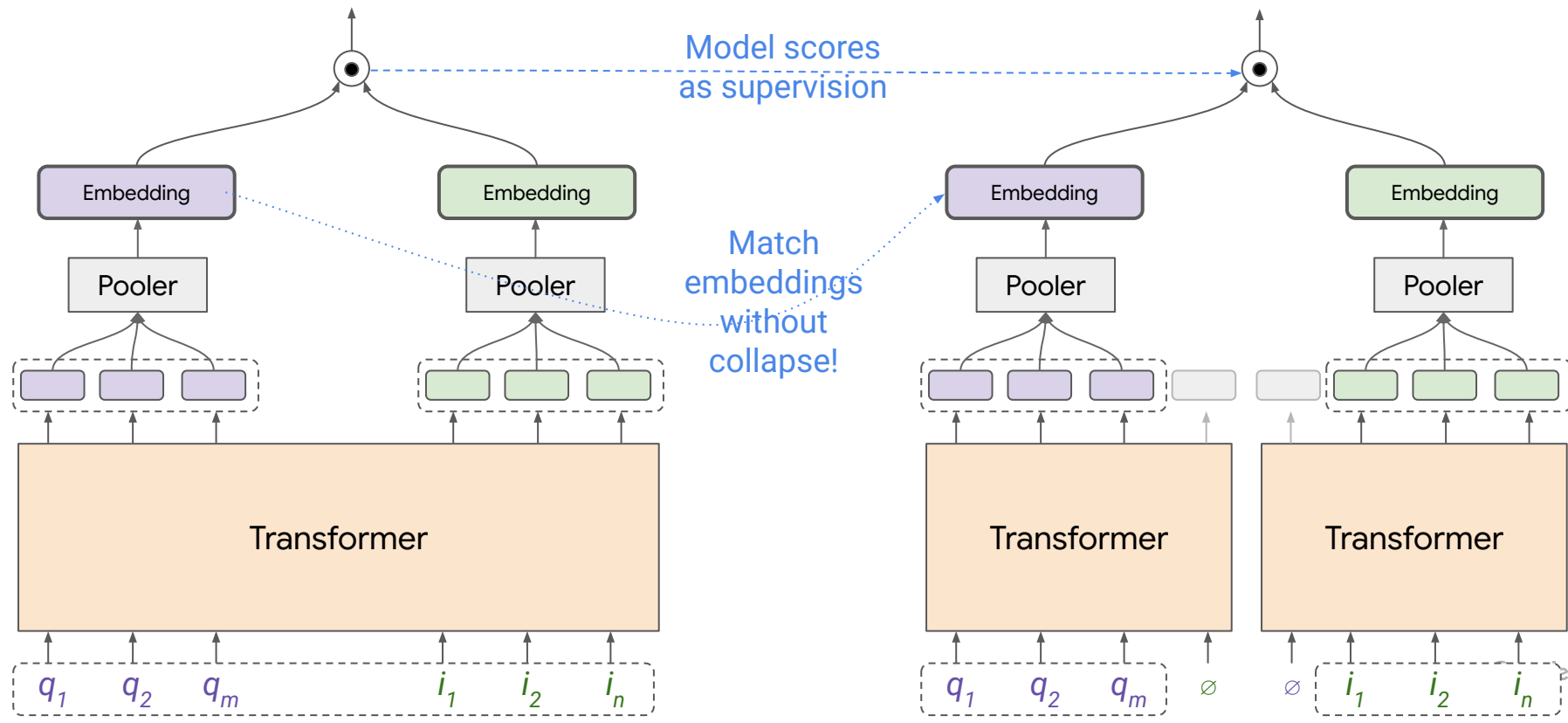
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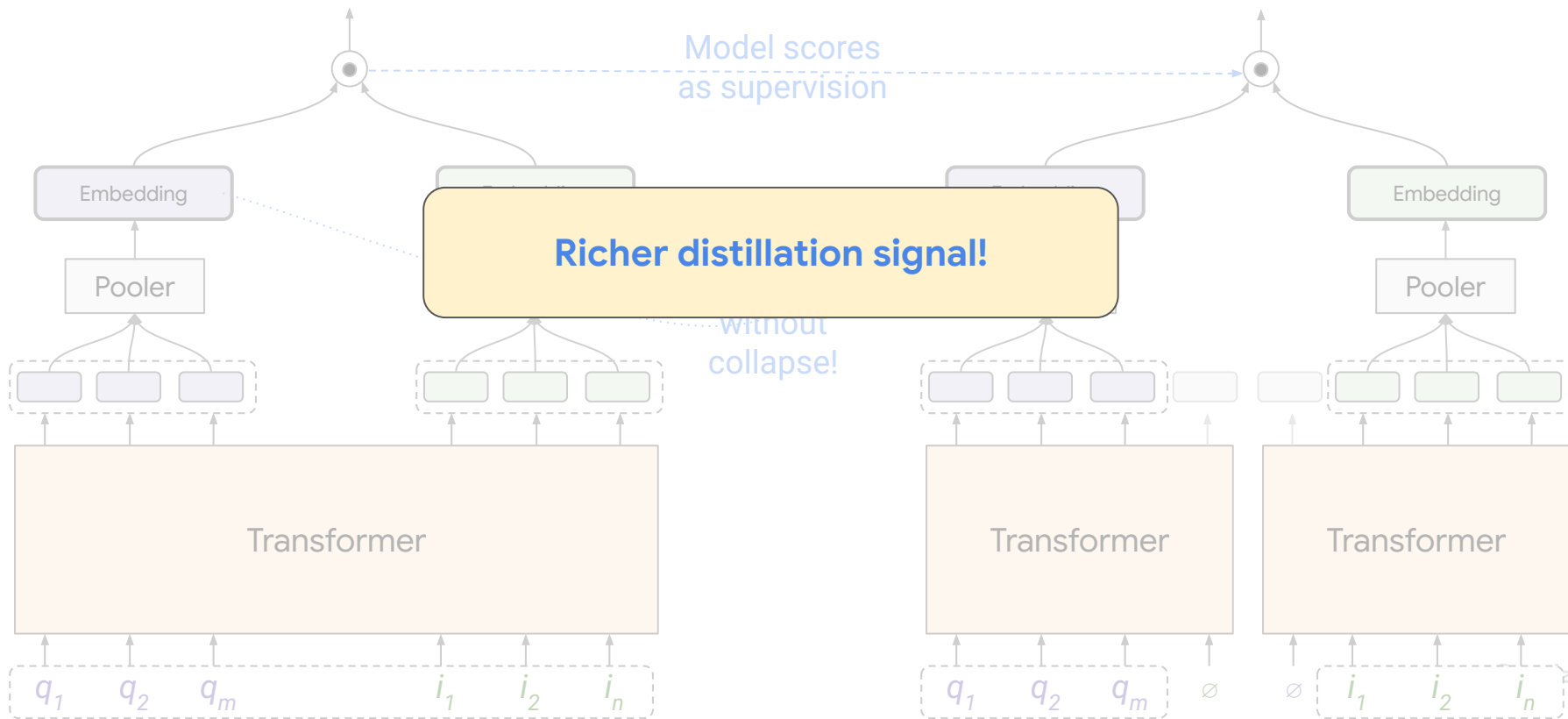
USTAD cross-encoder distillation

- Distill final scores **and** intermediate embeddings!



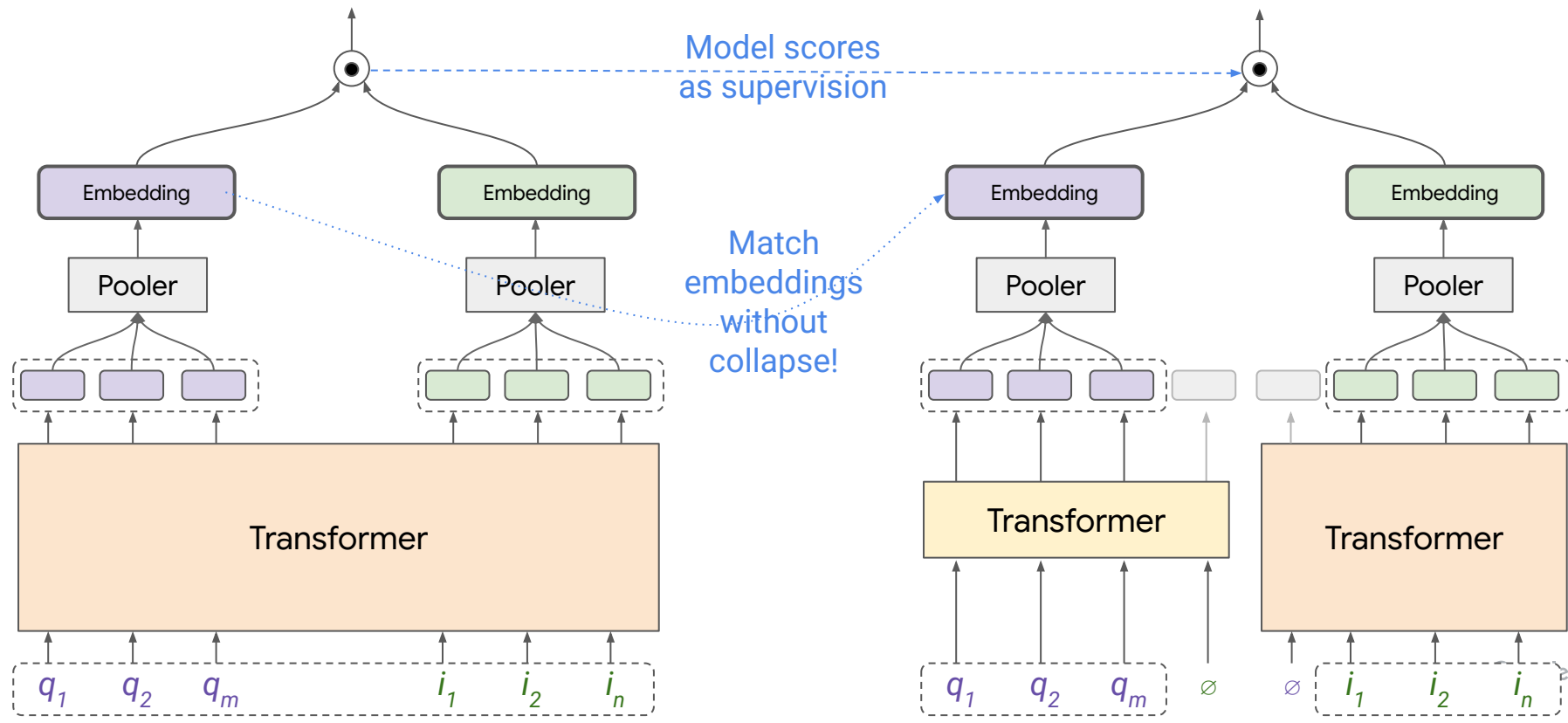
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- Distill final scores **and** intermediate embeddings!



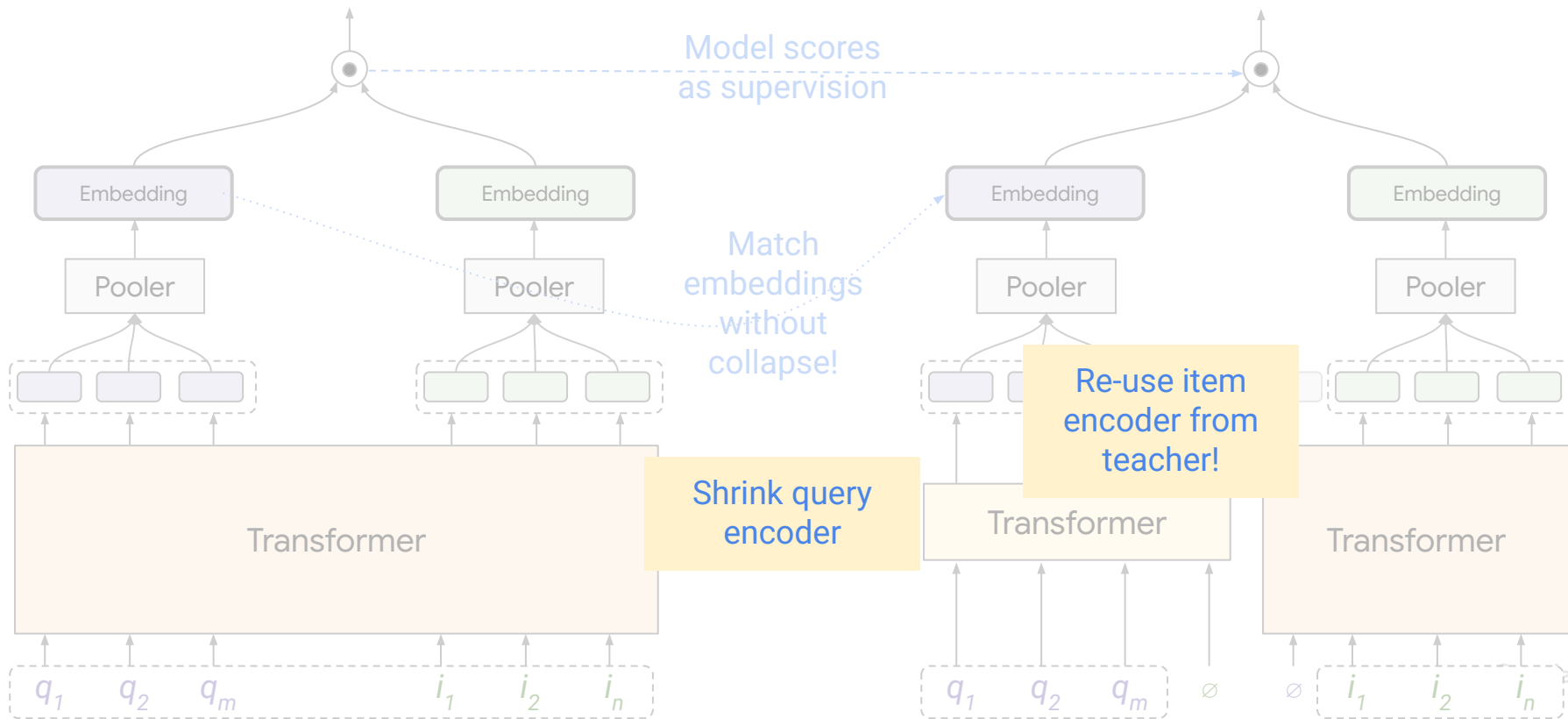
USTAD cross-encoder distillation + item tower re-use

- Distill final scores and intermediate embeddings!



USTAD cross-encoder distillation + item tower re-use

- Distill final scores and intermediate embeddings!



USTAD → smaller dual-encoder

- Embedding matching from USTAD teacher is powerful:

Dataset	Natural Questions (Dev)						MSMARCO (Dev)			
	67.5M			11.3M			67.5M		11.3M	
Method	R@1	R@5	R@10	R@1	R@5	R@10	MRR@10	nDCG@10	MRR@10	nDCG@10
Train student directly	39.5	66.4	74.7	34.1	59.8	68.6	27.0	32.2	23.0	29.7

Table 2. Reranking performance of various student DE models on NQ and MSMARCO dev set, including symmetric DE model (67.5M or 11.3M transformer as both encoders) and asymmetric DE student model (67.5M or 11.3M transformer as query encoder and document embeddings inherited from USTAD teacher). **The USTAD teacher achieves R@1 = 47.4, R@5 = 77.2, R@10 = 83.7, on NQ and MRR@10 = 40.0, nDCG@10 = 45.8 on MSMARCO.**

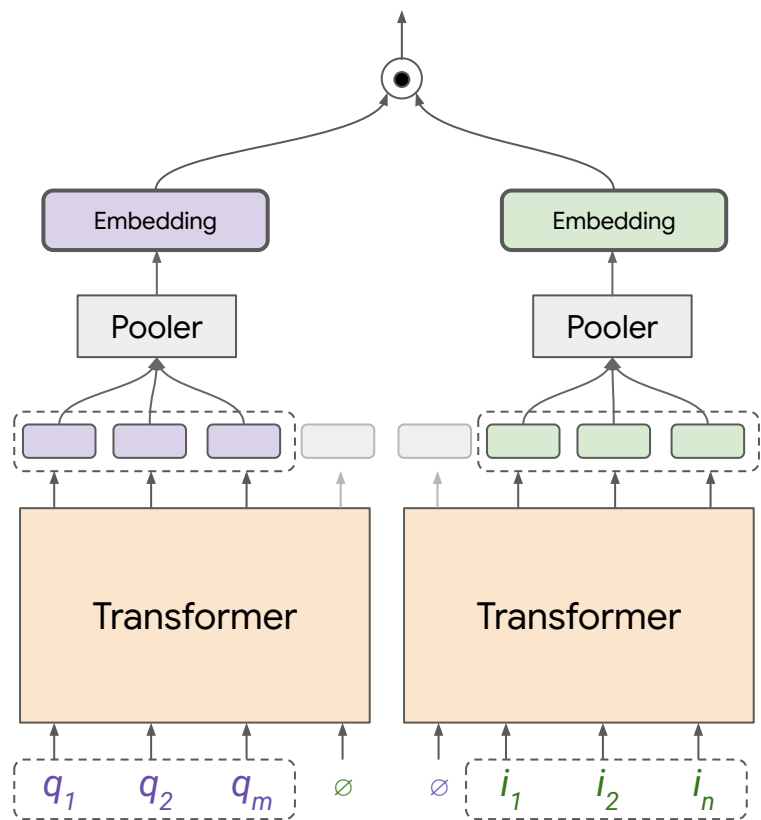
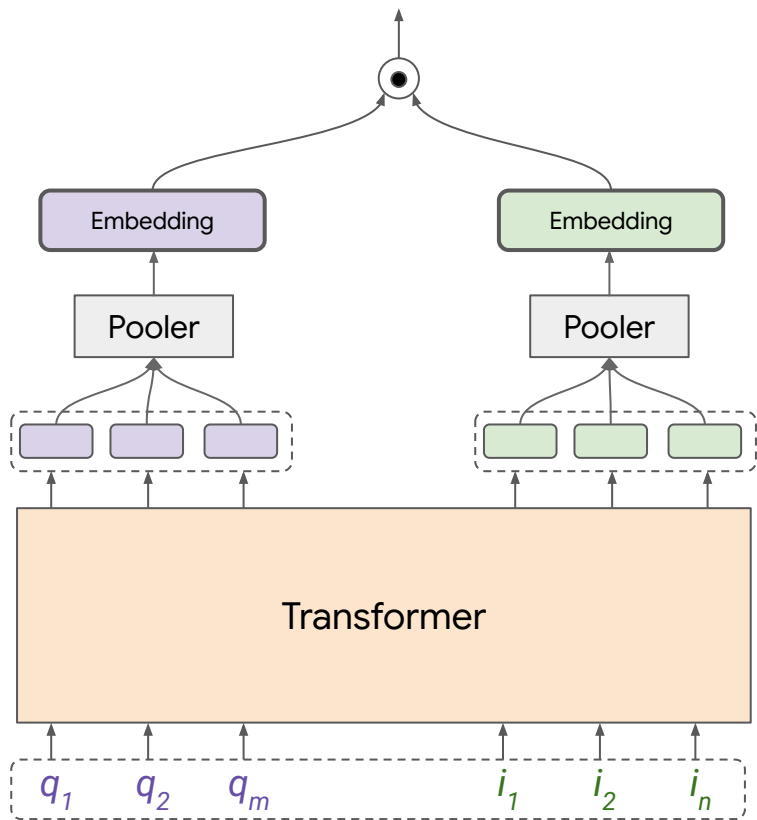
Generic dual-encoder → smaller dual-encoder

- Embedding matching from generic dual-encoder teacher (e.g., SentenceBERT) also shows gains:

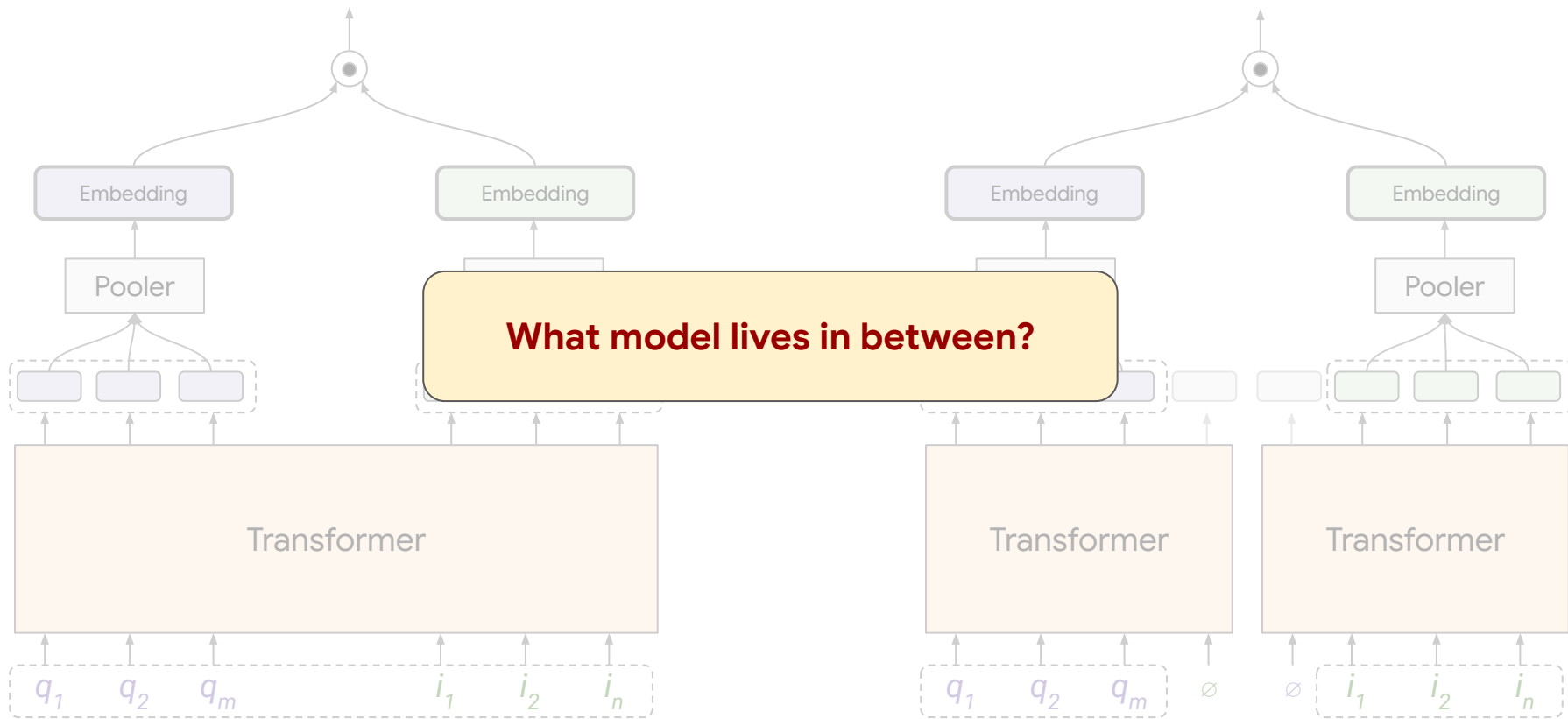
Dataset	Natural Questions (Dev)						MSMARCO (Dev)			
	67.5M			11.3M			67.5M		11.3M	
Method	R@5	R@20	R@100	R@5	R@20	R@100	MRR@10	nDCG@10	MRR@10	nDCG@10
Train student directly	36.2	59.7	80.0	24.8	44.7	67.5	22.6	27.2	18.6	22.5

Table 4. Retrieval performance (full recall against all documents in the corpus) of various student DE models on NQ and MSMARCO dev set, including symmetric DE model (67.5M or 11.3M transformer as both encoders) and asymmetric DE student model. **Teacher achieved R@5 = 72.3, R@20 = 86.1, and R@100 = 93.6 on NQ and MRR@10 = 37.2 and nDCG@10 = 44.2 on MSMARCO.**

USTAD: cross- and dual-encoder mode



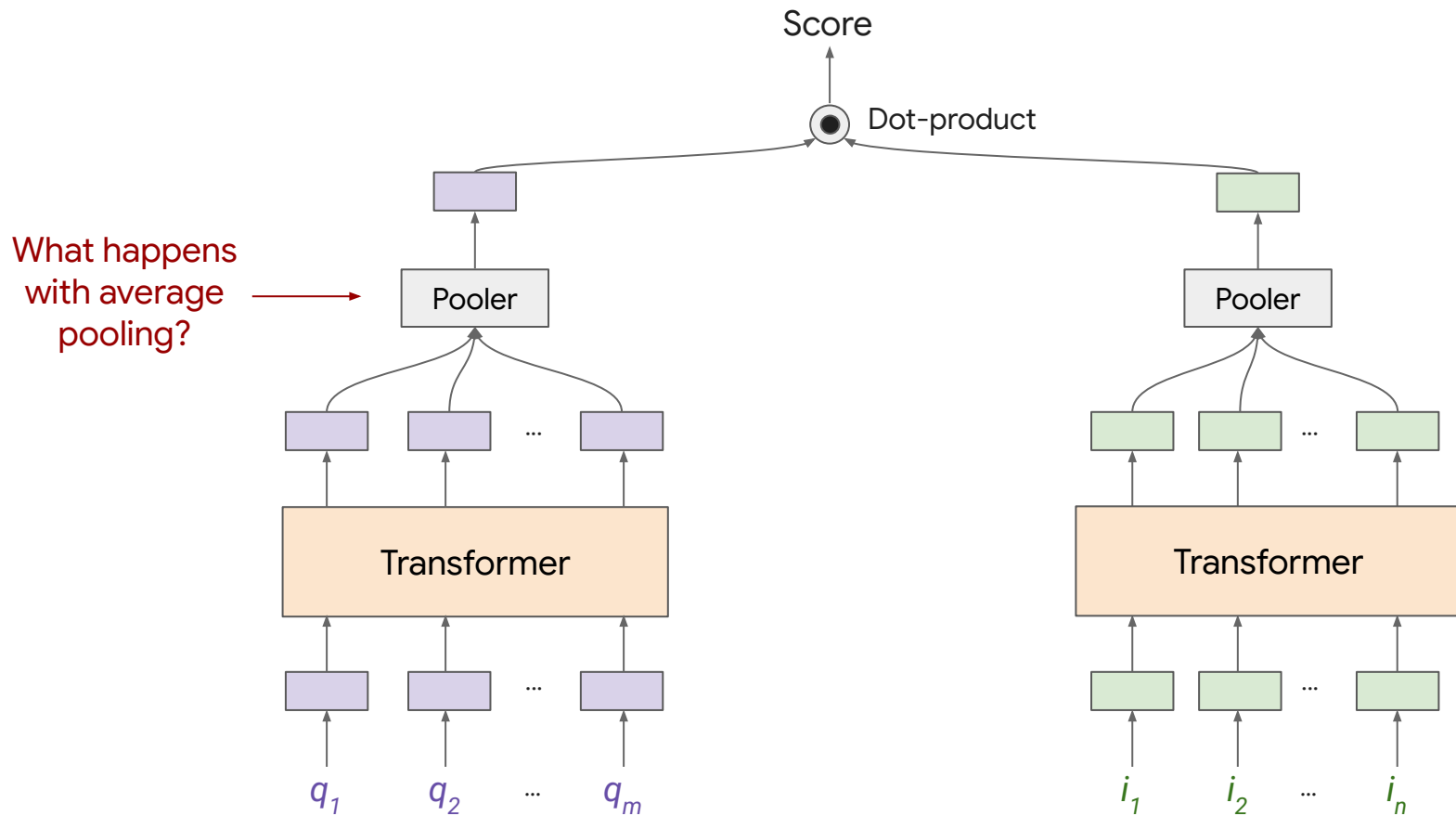
USTAD: cross- and dual-encoder mode



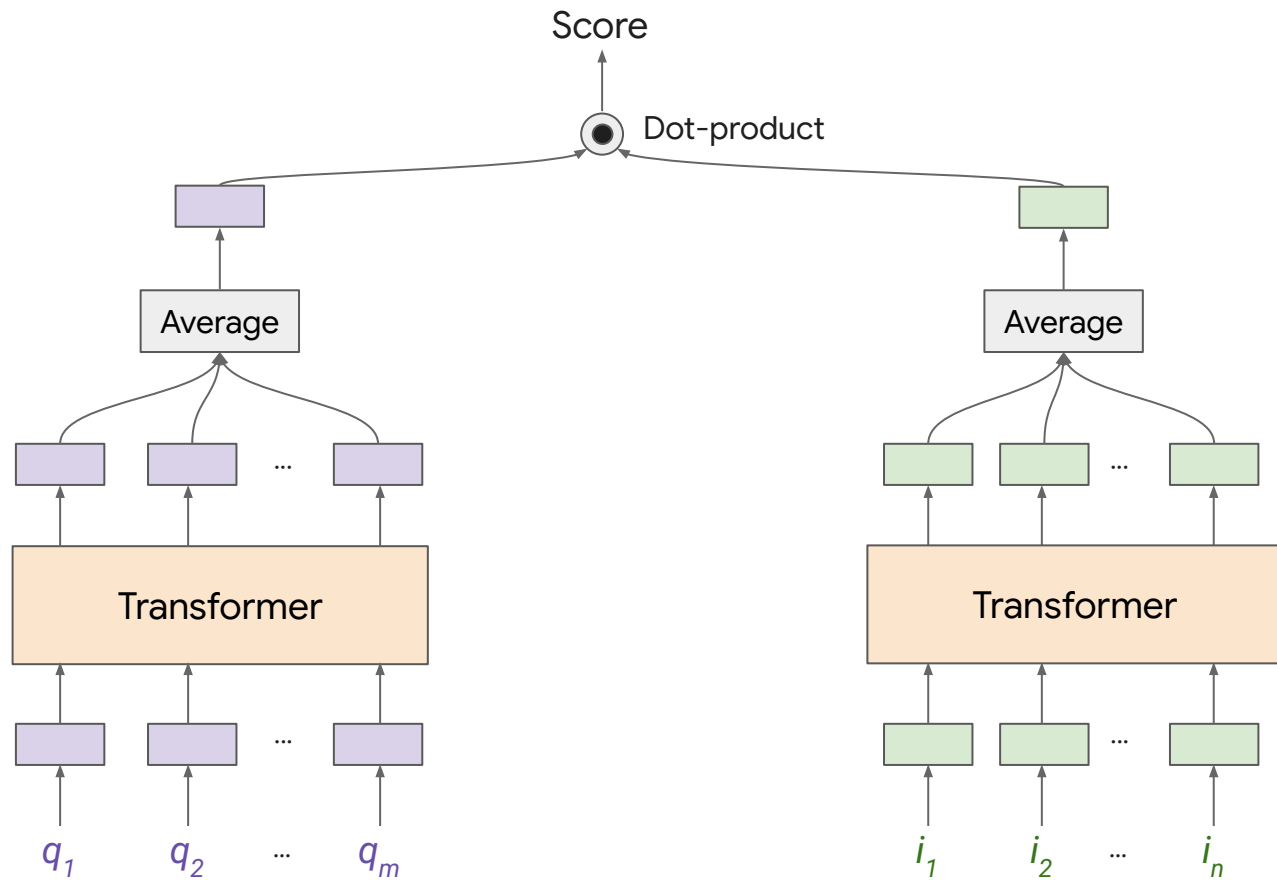
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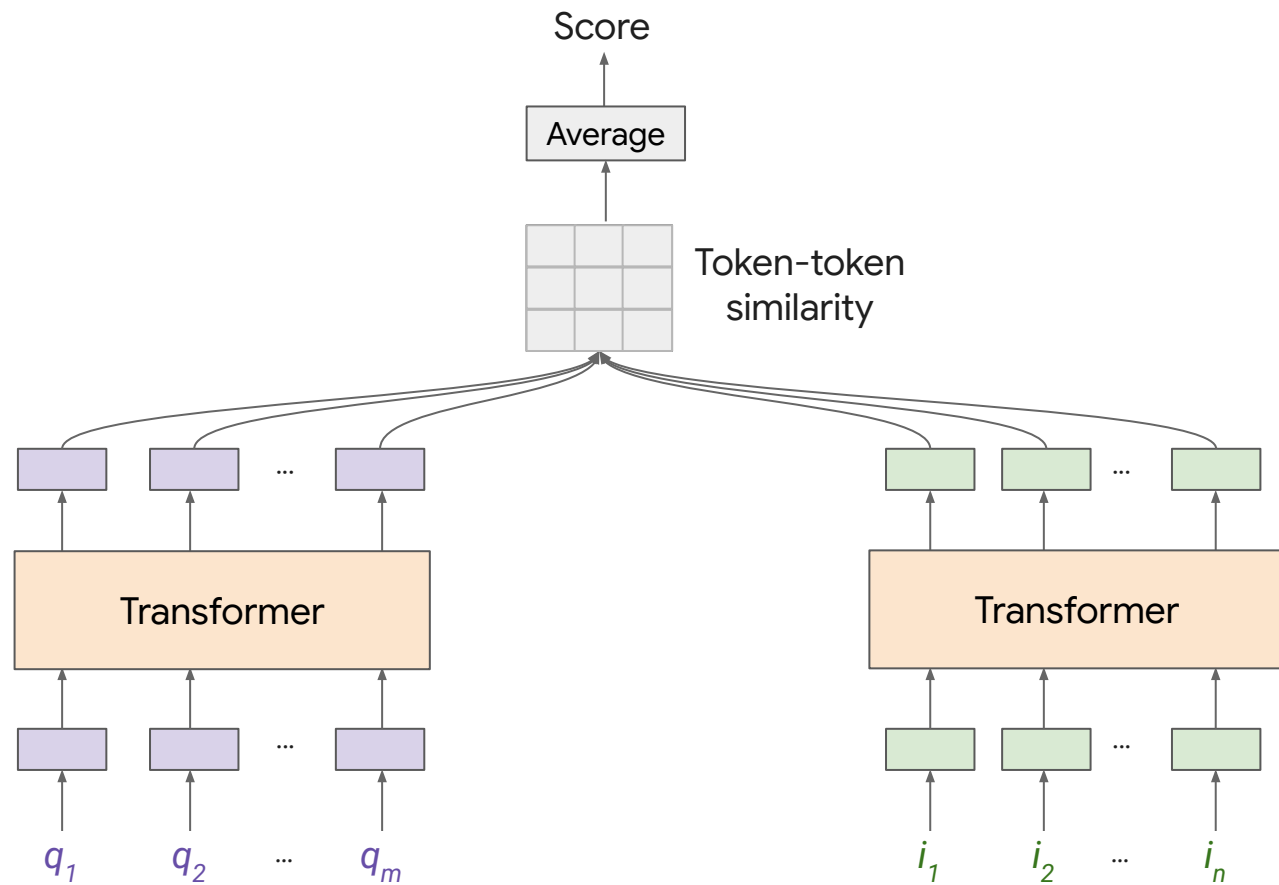
Dual-encoder: recap



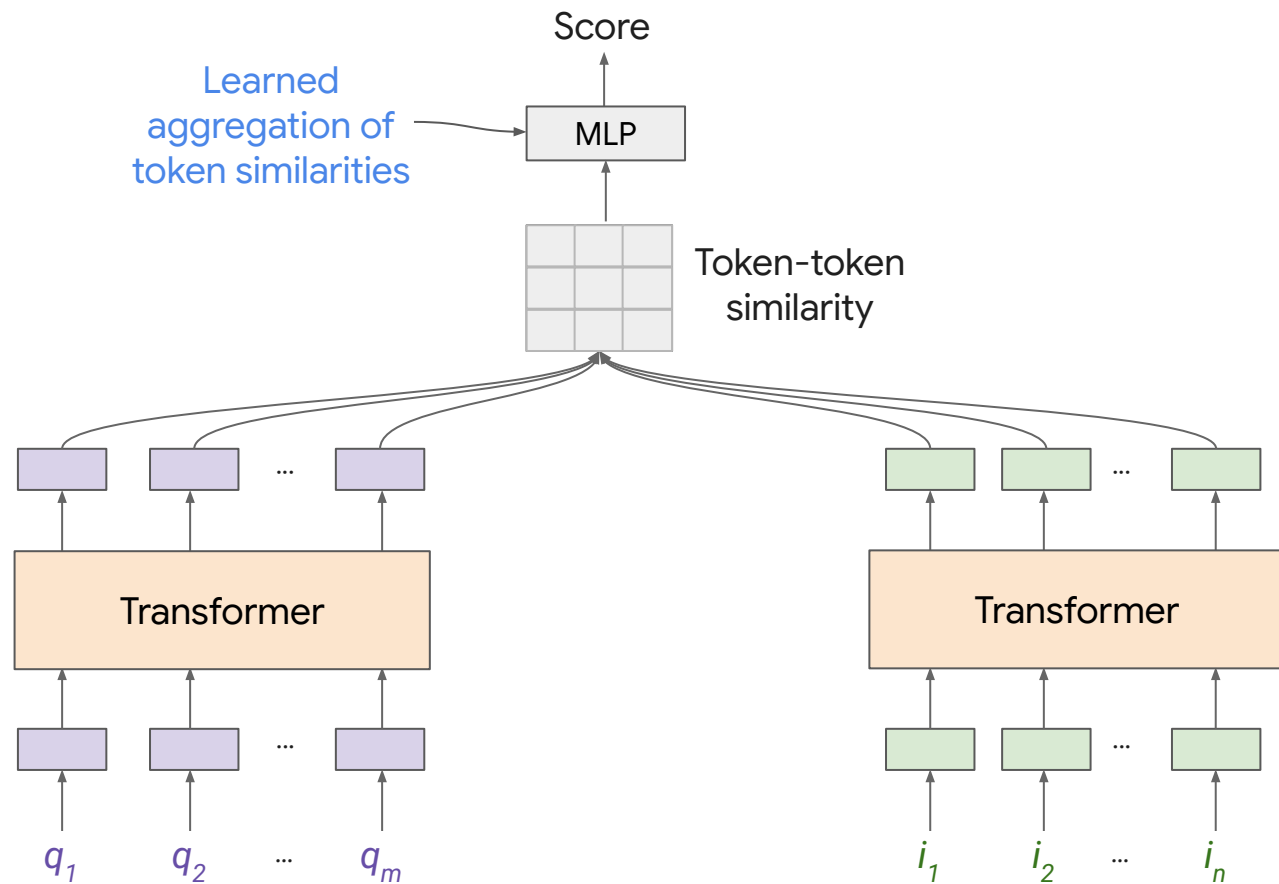
A closer look at average pooling



A closer look at average pooling

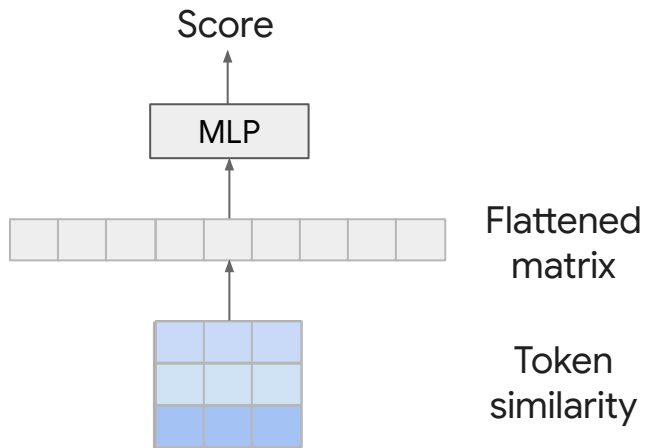


Learnable late-interaction (LITE)



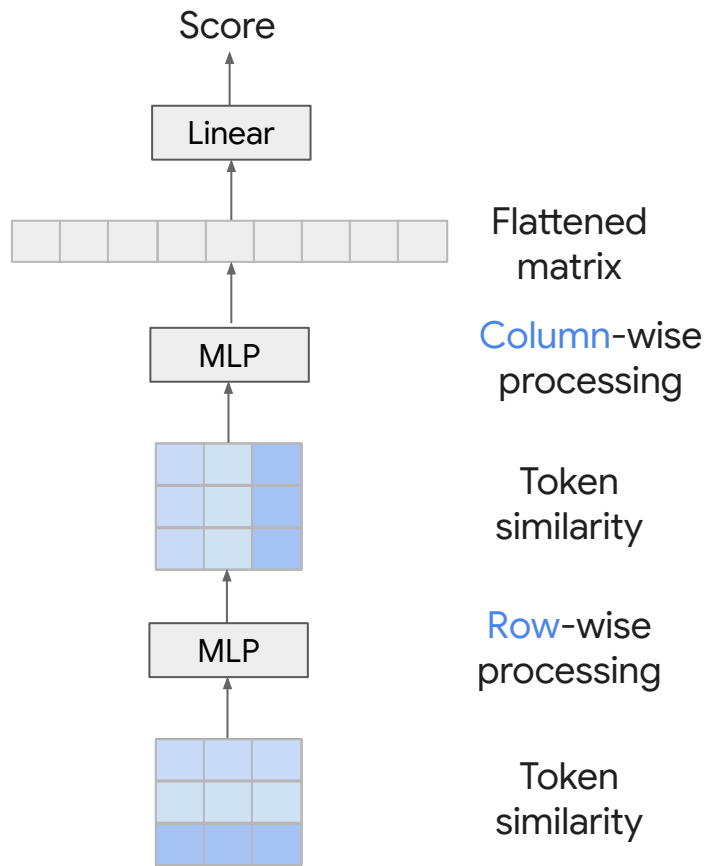
A closer look at the MLP

- **Flattened** LITE: operate on flattened token similarities



A closer look at the MLP

- **Separable** LITE: alternately process rows & columns
- MLP-Mixer style



Comparison to ColBERT

- ColBERT is a canonical late-interaction model, of the form:

$$s(q, i) = \sum_a \max_b q_a^\top i_b$$

- This involves a **fixed** aggregation of query and item tokens
 - May not be appropriate in all settings
- On the other hand, ColBERT is amenable to **retrieval** as well

Approximation power of dual-encoders

- Can dual-encoders fit any (reasonable) relevance function?
- **Yes**, with sufficiently high embedding dimension!

Proposition. Under mild technical conditions, any continuous query-item score function $s(q, i)$ can be approximated by some $Z(q)^T W(i)$, where $Z(q)$, $W(i)$ have at most **countably infinite** dimension.

- But what if the embedding size is restricted?

Approximation limits of dual-encoders

- Dual-encoders cannot approximate arbitrary functions with a restricted dimension!
 - Embedding dimension needs to scale with the sequence length

Proposition. Suppose queries and items are represented as length L sequences in some P embedding space. There exists a continuous function $s(q, i)$ such that, for any encoders $Z(q)$, $W(d)$ into some $Q < PL$ dimensional space, $Z(q)^\top W(d)$ suffers a **constant approximation error** against s .

Approximation power of LITE

- On the other hand, LITE turns out to be a universal approximator!
- Notably:
 - Without position encodings, result holds (CoBERT fails in this case)
 - With position encodings, result holds over (two!) pooled tokens' similarity

Proposition. Suppose queries and items are represented as length L sequences in some P embedding space. For any continuous function $s(q, i)$, there is a LITE model (i.e., Transformer + MLP) that can approximate s up to arbitrary precision.

Experiments: in-domain re-ranking

- LITE effectively interpolates between cross- & dual-encoders

Scorer	Latency (in ms)	Storage	MS MARCO MRR@10
CE (student)	10990	0×	0.395
DE	42	1×	0.355
ColBERT	62	200×	0.383
Separable LITE	111	200×	0.393
Small sep LITE	56	50×	0.391

← Highest quality, but highest cost

4x less document tokens

Scorer	MS MARCO		DL 2019		DL 2020		NQ	
	MRR	nDCG	MRR	nDCG	MRR	nDCG	MRR	nDCG
DE	0.355	0.413	0.861	0.744	0.842	0.723	0.699	0.611
ColBERT	0.383	0.442	0.878	0.753	0.860	0.731	0.756	0.689
Sep LITE	0.393	0.452	0.898	0.765	0.873	0.756	0.769	0.693

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Close to CE quality with much lower cost

4x less document tokens

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DE	0.355	0.413	0.861	0.744	0.842	0.723	0.699	0.611
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DE	42	1×	0.355
ColBERT	62	200×	0.383
Separable LITE	111	200×	0.393
Small sep LITE	56	50×	0.391

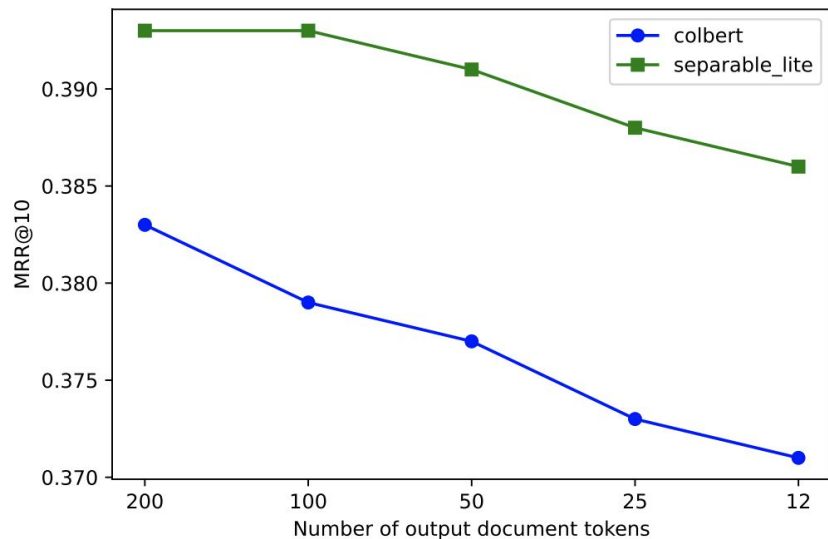
Significantly better than DE quality

4x less document tokens

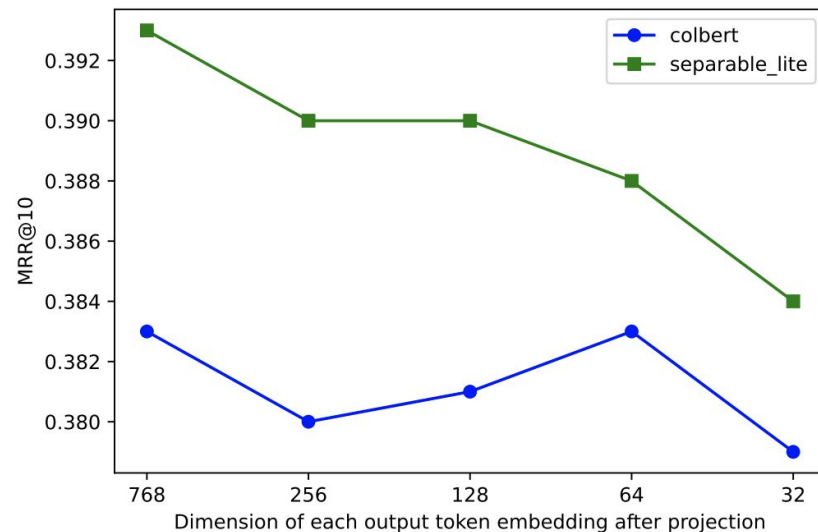
Scorer	MS MARCO		DL 2019		DL 2020		NQ	
	MRR	nDCG	MRR	nDCG	MRR	nDCG	MRR	nDCG
DE	0.355	0.413	0.861	0.744	0.842	0.723	0.699	0.611
ColBERT	0.383	0.442	0.878	0.753	0.860	0.731	0.756	0.689
Sep LITE	0.393	0.452	0.898	0.765	0.873	0.756	0.769	0.693

Experimental results: cost reduction

- Lightweight scoring methods require more storage than dual-encoders
- LITE performs well with pooling and/or reduced embedding size!



Reduction via local averaging or projection



Reduction via projection

Experiments: out-of-domain re-ranking

- LITE shows consistently good generalisation on BEIR tasks

Dataset	ColBERT	Sep LITE	CE
T-COVID	0.761	0.763	0.771
NFCorpus	0.356	0.358	0.361
NQ	0.525	0.540	0.552
HotpotQA	0.685	0.681	0.728
FiQA-2018	0.330	0.336	0.346
ArguAna	0.433	0.424	0.519
Touché-2020	0.274	0.305	0.300
CQAD	0.363	0.374	0.378
Quora	0.767	0.839	0.832
DBPedia	0.410	0.434	0.438
SCIDOCS	0.155	0.164	0.167
FEVER	0.782	0.788	0.804
C-FEVER	0.190	0.213	0.232
SciFact	0.667	0.633	0.695

Agenda

- 01 A (neural) retrieval primer
- 02 Limits of dual encoders
- 03 Unified cross & dual encoders
- 04 Hybrid cross & dual encoders
- 05 **Conclusion & future work**

Cross- versus dual-encoders

Dual-encoders tend to underperform for **re-ranking**

Why does this happen?

Poorer margins

Expressivity with small dimension

What can we do about it?

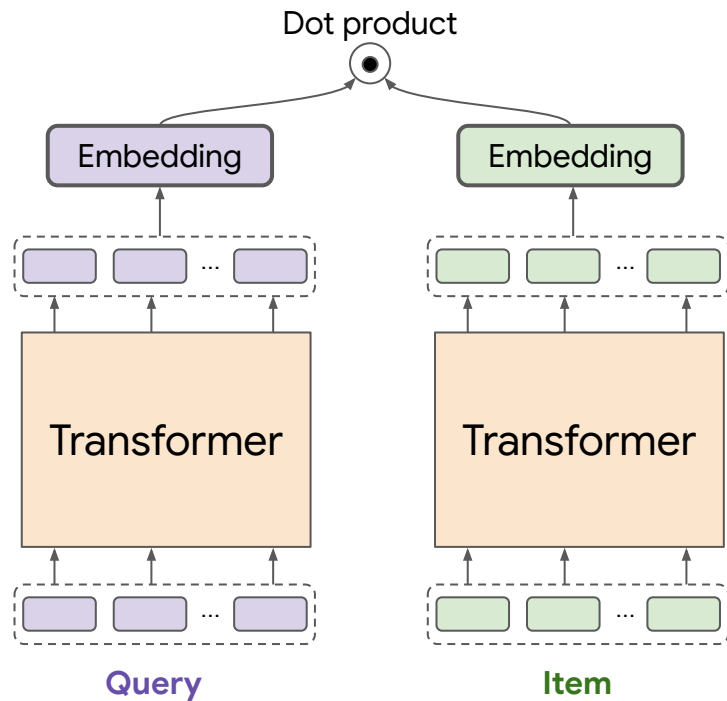
Score-based distillation

Architecture modification



Embedding-based distillation

Lightweight scoring



Future work

Further optimising the encoder (cost, quality) tradeoff

Can we get the best of both worlds?

Unified retrieval and re-ranking

Do we really need two phases?

Generative retrieval and re-ranking

Do we even need encoder models?!

Thank You

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